MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL **Strand 1: Number and Operations** CONCEPT 2008 PO ITEM DESCRIPTION 2003 PO ITEM DESCRIPTION 1. Number Sense Compare and order real numbers including Locate rational numbers on a number line. 1 very large and small integers, and decimals and fractions close to zero. 2 Classify real numbers as rational or 2 Identify irrational numbers. irrational. 3 Classify real numbers as rational or irrational. Model the relationship between the 3 M07-Classify rational numbers as natural, whole, or subsets of the real number system. S1C1-08 integers. Select the grade-level appropriate operation to 4 Model and solve problems involving 1 solve word problems. absolute value. Solve word problems using grade-level 2 appropriate operations and numbers. 2. Numerical 1 Solve problems with factors, multiples, 1 Select the grade-level appropriate operation to divisibility or remainders, prime numbers, **Operations** solve word problems. Solve word problems using grade-level and composite numbers. 2 appropriate operations and numbers. *Describe the effect of multiplying and 2 dividing a rational number by • a number less than zero, a number between zero and one. • one, and • a number greater than one.* Solve problems involving percent increase, 3 9 Calculate the missing value in a percentage percent decrease, and simple interest problem. rates. Convert standard notation to scientific 4 10 Convert standard notation to scientific notation, notation and vice versa (include positive and vice versa. and negative exponents).

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

Strand 1: Number and Operations				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
2. Numerical	5	Simplify numerical expressions using the	3	Determine the square of an integer.
Operations		order of operations that include grouping	4	Determine the square root of an integer.
		symbols, square roots, cube roots, absolute values, and positive exponents.	5	Identify squaring and finding square roots as inverse operations.
			7	Apply the symbols "√" to represent square root, "±" to represent roots, and "{}" as grouping symbols.
			11	Simplify numerical expressions using the order of operations with grade appropriate operations on number sets.
	M08- S3C3-03	Moved to Strand 3 Concept 3	6	Apply grade-level appropriate properties to assist in computation.
		REMOVED (This skill is required throughout the standard.)	8	Use grade-level appropriate mathematical terminology.
3. Estimation	1	Make estimates appropriate to a given situation.	1	Solve grade-level appropriate problems using estimation.
			2	Use estimation to verify the reasonableness of a calculation (e.g., Is 32 the square root of 64?).
			3	Express answers to the appropriate place or degree of precision (e.g., time, money).
			4	Verify the reasonableness of estimates made from calculator results within a contextual situation.
	2	Estimate the location of rational and	M08-	Locate rational numbers on a number line.
	_	common irrational numbers on a number	S1C1-01	
		line.	M08-	Identify irrational numbers.
			S1C1-02	

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

Strand 2: Data Analysis, Probability, and Discrete Mathematics				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
1. Data Analysis (Statistics)	1	Solve problems by selecting, constructing,	2	Construct box-and-whisker plots.
(Statistics)		interpreting, and calculating with displays of data, including box and whisker plots	4	Interpret box-and-whisker plots, circle graphs, and scatter plots.
		and scatterplots.	9	Solve contextual problems using scatter plots, box-and-whiskers plots, and double line graphs of continuous data.
			3	Determine the appropriate type of graphical display for a given data set.
			5	Answer questions based on box-and-whisker plots, circle graphs, and scatter plots.
			7	Formulate reasonable predictions based on a given set of data.
			11	Identify a line of best fit for a scatter plot.
	2	2 Make inferences by comparing the same summary statistic for two or more data sets.	6	Solve problems in contextual situations using the mean, median, mode, and range of a given data set.
			8	Compare trends in data related to the same investigation.
			11	Identify a line of best fit for a scatter plot.
	3	Describe how summary statistics relate to the shape of the distribution.	6	Solve problems in contextual situations using the mean, median, mode, and range of a given data set.
	4	Determine whether information is represented effectively and appropriately given a graph or a set of data by	3	Determine the appropriate type of graphical display for a given data set.
		identifying sources of bias and compare and contrast the effectiveness of different representations of data.	MHS- S2C1-17	Identify differences between biased and unbiased samples.
	5	*Evaluate the design of an experiment.*		

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

CONCEPT	2000 DO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
	2008 PO		_	
1. Data Analysis (Statistics)		REMOVED	1	Formulate questions to collect data in contextual situations.
		REMOVED	10	Evaluate the effects of missing or incorrect data on the results of an investigation (e.g., Susie's teacher recorded a 39 instead of a 93 for her last quiz, what will happen to Susie's average?).
	MCWR- S2C1-07	Moved to College Work Readiness	12	Distinguish between causation and correlation.
2. Probability	1	Determine theoretical and experimental conditional probabilities in compound probability experiments.	1	Determine the probability that a specific event will occur in a 2-stage probability experiment.
			3	Predict the outcome of a grade-level appropriate probability experiment.
	2	Interpret probabilities within a given context and compare the outcome of an experiment to predictions made prior to performing the experiment.	2	Solve contextual situations using probability (e.g., If the probability of Michelle making a free throw is 0.25, what is the probability that she will make three free throws in a row?).
			4	Record the data from performing a grade-level appropriate probability experiment.
			5	Compare the outcome of an experiment to predictions made prior to performing the experiment.
			7	Compare the results of two repetitions of the same grade-level appropriate probability experiment.
	3	Use all possible outcomes (sample space) to determine the probability of dependent and independent events.	6	Distinguish between independent and dependent events.

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

	Strand 2: Data Analysis, Probability, and Discrete Mathematics					
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION		
3. Systematic Listing and Counting	1	Represent, analyze, and solve counting problems with or without ordering and repetitions.	2	Determine all possible outcomes involving the combination of two or more sets of objects (e.g., If you roll a six-sided number cube 4 times, how many possible outcomes are possible?). Determine all possible arrangements given a set (e.g., How many ways can you arrange a set of 7 books on a shelf?).		
	2	*Solve counting problems and represent counting principles algebraically including factorial notation.*				
4. Vertex-Edge Graphs	1	Use directed graphs to solve problems.	1	Solve contextual problems represented by vertexedge graphs.		

	Strand 3: Patterns, Algebra, and Functions				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION	
1. Patterns	1	Recognize, describe, create, and analyze numerical and geometric sequences using	1	Communicate a grade-level appropriate iterative or recursive pattern, using symbols or numbers.	
		tables, graphs, words, or symbols; make conjectures about these sequences.	2	Extend a grade-level appropriate iterative or recursive pattern.	
			3	Solve grade-level appropriate iterative or recursive pattern problems.	
2. Functions and Relationships	1	Sketch and interpret a graph that models a given context; describe a context that is modeled by a given graph.	1	Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).	
			3	Determine whether a graph or table is related to a given equation of the form $y=ax^2$ where 'a' is a natural number.	
			M08- S4C3-01	Use a table of values to graph a linear equation.	

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

	Strand 3: Patterns, Algebra, and Functions				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION	
2. Functions and Relationships	2	*Determine if a relationship represented by a graph or table is a function.*			
	3	Write the rule for a simple function using algebraic notation.	4	Identify independent and dependent variables for a contextual situation.	
			M07- S3C2-01	Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).	
	4	Identify functions as linear or nonlinear and contrast distinguishing properties of functions using equations, graphs, or tables.	2	Distinguish between linear and nonlinear functions, given graphic examples.	
	5	*Demonstrate that proportional relationships are linear using equations, graphs, or tables.*			
3. Algebraic	1	Write or identify algebraic expressions,	2	Use variables in contextual situations.	
Representations		equations, or inequalities that represent a situation.	5	Translate a contextual situation into an algebraic inequality (e.g., Joe earns more than \$5.00 an hour; therefore, <i>x</i> > 5).	
			6	Identify an equation or inequality that represents a contextual situation.	
	2	Evaluate an expression containing variables by substituting rational numbers for the variables.	1	Evaluate algebraic expressions by substituting rational values for variables [e.g., $2(ab+ac+bc)$, when $a = 2$, $b = 3/5$, and $c = 4$].	

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

Strand 3: Patterns, Algebra, and Functions				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
3. Algebraic Representations	3	Analyze situations, simplify, and solve problems involving linear equations and	7	Solve one-step equations with rational numbers as coefficients or as solutions.
·		inequalities using the properties of the real number system.	8	Solve one-step equations that model contextual situations.
			9	Solve two-step equations with rational coefficients and integer solutions (e.g., $3x + 5 = 11$, $4x - 20 = 8$).
			M08- S1C2-06	Apply grade-level appropriate properties to assist in computation.
	4	Translate between different representations of linear equations using symbols, graphs, tables, or written	3	Translate a written sentence or phrase into an algebraic equation or expression, and vice versa (e.g., Three less than twice a number is 2 <i>n</i> -3.).
		descriptions.	4	Translate a sentence written in context into an algebraic equation involving two operations.
	5	Graph an inequality on a number line.	10	Graph an inequality on a number line.
	M08- S4C4-02	Moved to Strand 4 Concept 4	11	Solve a simple algebraic proportion.
	M08- S4C3-02	Moved to Strand 4 Concept 3	12	Solve applied problems using the Pythagorean theorem.
4. Analysis of Change	1	Interpret the relationship between a linear equation and its graph, identifying and computing slope and intercepts.	1	Identify the slope of a line as the rate of change (the ratio of rise over run).
	2	Solve problems involving simple rates.	M08- S5C1-01	Describe how to use a proportion to solve a problem in context.

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

	Strand 4: Geometry and Measurement				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION	
1. Geometric Properties	1	Identify the attributes of circles: radius, diameter, chords, tangents, secants,	7	Recognize the relationship between inscribed angles and intercepted arcs.	
		inscribed angles, central angles, intercepted arcs, circumference, and area.	8	Identify tangents and secants of a circle.	
	2	*Predict results of combining, subdividing, and changing shapes of plane figures and solids.*			
	3	Use proportional reasoning to determine congruence and similarity of triangles.	1	Draw a model that demonstrates basic geometric relationships such as parallelism, perpendicularity, similarity/proportionality, and congruence.	
			10	Identify corresponding angles of similar polygons as congruent and sides as proportional.	
			M08- S4C4-06	Solve problems using ratios and proportions, given the scale factor.	
			M08- S4C4-07	Calculate the length of a side, given two similar triangles.	
	4	*Use the Pythagorean Theorem to solve problems.*			
	M07- S4C1-03	Moved to Grade 7	1	Draw a model that demonstrates basic geometric relationships such as parallelism, perpendicularity, similarity/proportionality, and congruence.	
	M07- S4C1-03	Moved to Grade 7	2	Draw 3-dimensional figures by applying properties of each (e.g., parallelism, perpendicularity, congruency).	
	M04- S4C1-07	Moved to Grade 4	3	Recognize the 3-dimensional figure represented by a net.	
	M07- S4C4-05	Moved to Grade 7	4	Represent the surface area of rectangular prisms and cylinders as the area of their net.	

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

Strand 4: Geometry and Measurement				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
1. Geometric Properties	M05- S4C1-01	Moved to Grade 5	5	Draw regular polygons with appropriate labels.
	M07- S4C1-02	Moved to Grade 7	6	Identify the properties of angles created by a transversal intersecting two parallel lines (e.g., corresponding angles are congruent).
	MHS- S4C1-09	Moved to High School	9	Determine whether three given lengths can form a triangle.
2. Transformation of Shapes	1	Model the result of rotations in multiples of 45 degrees of a 2-dimensional figure about the origin.	2	Model a simple transformation on a coordinate grid (e.g., Translate right four units and down two units.).
	2	Describe the transformations that create a given tessellation.	M05- S4C2-02	Describe the transformations that created a tessellation.
	3	*Identify lines of symmetry in plane figures or classify types of symmetries of 2-dimensional figures.*		
	M06- S4C2-01	Moved to Grade 6	1	Identify the planar geometric figure that is the result of a given rigid transformation.
3. Coordinate Geometry	1	Make and test a conjecture about how to find the midpoint between any two points in the coordinate plane.	2	Determine the midpoint given two points on a number line.
	2	Use the Pythagorean Theorem to find the distance between two points in the	3	Determine the distance between two points on a number line.
		coordinate plane.	M08- S3C3-12	Solve applied problems using the Pythagorean theorem.
	M08- S3C2-01	Moved to Strand 3 Concept 2	1	Use a table of values to graph a linear equation.
4. Measurement	1	*Solve problems involving conversions within the same measurement system.*		

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

	Strand 4: Geometry and Measurement				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION	
4. Measurement	2	Solve geometric problems using ratios and proportions.	6	Solve problems using ratios and proportions, given the scale factor.	
			7	Calculate the length of a side, given two similar triangles.	
			M08- S5C1-01	Describe how to use a proportion to solve a problem in context.	
			M08- S3C3-11	Solve a simple algebraic proportion.	
	3	Calculate the surface area and volume of rectangular prisms, right triangular	2	Solve problems involving the volume of rectangular prisms and cylinders.	
		prisms, and cylinders.	3	Calculate the surface area of rectangular prisms or cylinders.	
			4	Identify rectangular prisms and cylinders having the same volume.	
	M06- S4C4-05	Moved to Grade 6	1	Solve problems for the area of a trapezoid.	
	MHS- S4C1-06	Moved to Grade HS	5	Find the measure of a missing interior angle in a triangle or quadrilateral.	

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

Strand 5: Structure and Logic				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
1. Algorithms and Algorithmic	1	Create an algorithm to solve problems involving indirect measurements, using	1	Describe how to use a proportion to solve a problem in context.
Thinking		proportional reasoning, dimensional analysis, and the concepts of density and rate.	M08- S4C4-06	Solve problems using ratios and proportions, given the scale factor.
	M06- S5C1-01	Moved to Grade 6	2	Analyze algorithms.
2. Logic, Reasoning, Problem Solving, and Proof	1	*Analyze a problem situation to determine the question(s) to be answered.*		
	2	*Analyze and compare mathematical strategies for efficient problem solving; select and use one or more strategies to solve a problem.*	M08- S1C2-01	Select the grade-level appropriate operation to solve word problems.
			M08- S1C2-02	Solve word problems using grade-level appropriate operations and numbers.
	3	*Identify relevant, missing, and extraneous information related to the solution to a problem.*		
	4	*Represent a problem situation using multiple representations, describe the process used to solve the problem, and verify the reasonableness of the solution.*	3	Model a contextual situation using a flow chart.
	5	*Apply a previously used problem- solving strategy in a new context.*		
	6	*Communicate the answer(s) to the question(s) in a problem using appropriate representations, including symbols and informal and formal mathematical language.*		

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

	Strand 5: Structure and Logic				
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION	
2. Logic, Reasoning, Problem Solving, and Proof	7	*Isolate and organize mathematical information taken from symbols, diagrams, and graphs to make inferences, draw conclusions, and justify reasoning.*			
	8	Describe when to use proportional reasoning to solve a problem.	M08- S5C1-01	Describe how to use a proportion to solve a problem in context.	
	9	*Make and test conjectures based on information collected from explorations and experiments.*			
	10	Solve logic problems involving multiple variables, conditional statements, conjectures, and negation using words, charts, and pictures.	1	Solve a logic problem given the necessary information.	
	11	Identify simple valid arguments using if then statements.	2	Identify simple valid arguments using ifthen statements (e.g., All squares are rectangles. If quadrilateral ABCD is a rectangle, is it a square?).	
	12	*Make, validate, and justify conclusions and generalizations about linear relationships.*			
	13	Verify the Pythagorean Theorem using a valid argument.	4	Verify the Pythagorean theorem using an area dissection argument.	

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.